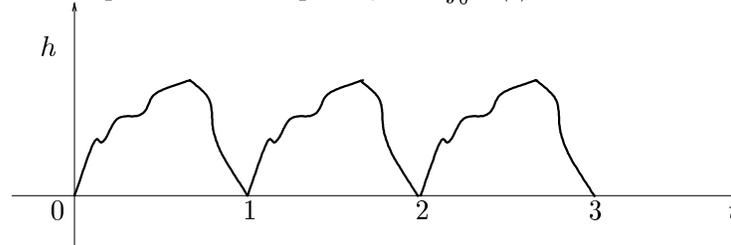


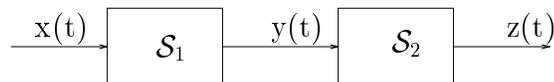
1. We consider a linear, time invariant system with impulse response $h(t)$ depicted in the figure. The function is made of three identical curves in the intervals $[0, 1]$, $[1, 2]$, $[2, 3]$, and is zero outside that range. It is non-negative, and $\int_0^1 h(t)dt = 1$.



Sketch the response of the system to the input $x(t) = u(t) - u(t - 1)$.

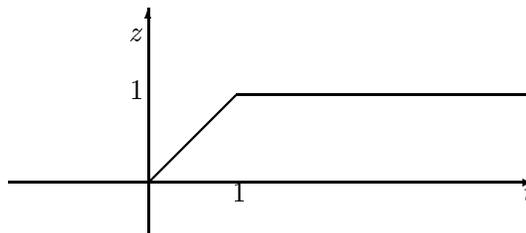
Your sketch cannot be exact since you don't know $h(t)$ exactly, but it must be consistent with the information given above.

2. Given the function $f(t) = e^{-t}u(t)$, where $u(t)$ is the step function, find the convolutions:
- $u * f$;
 - $f * f$;
 - $u * u$.
3. Consider the cascade of linear, time-invariant systems \mathcal{S}_1 and \mathcal{S}_2 .



We know:

- The impulse response function $h_1(t) = u(t) - u(t - 2)$.
- The response of system \mathcal{S}_2 to the ramp input $y(t) = tu(t)$ is the function $z(t)$ below.



Find and sketch the impulse response of the cascade.